Grade: 11 (TOEFL-Beginner)

Subject: Mathematics

Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
Δυσ	2		Patterns	Chapter 1: Sequences	• Understand what	e Group Work	Croup Procentations
Aug.	2	AERO HSS.CP.9 (+)	Patterns, Functions, and Algebra	Chapter 1: Sequences Unit 1: Introduction • Functions • Definition • Substitution • Composition of functions • Sums • Definition and notation • Finite Sums • Products • Definition and notation • Finite Products	 Understand what functions are Understand how to substitute both constants and variables into given functions Understand how to compose functions and that function composition is not commutative Understand the notation for finite sums and how to calculate them Understand the notation for finite products and how to calculate them 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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The Asian International School Curriculum Mapping <u>Subject: Mathematics</u>

Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
	5	AERO HSS.CP.9 (+) AERO HSAAPR.5 (+)	Patterns, Functions, and Algebra	Chapter 1: Sequences Unit 2: Combinatorics • Factorial: $n! = 1 \cdot 2 \cdots n = \prod_{j=1}^{n}$ 0! = 1! = 1 • Permutation: $P(n,r) = {}_{n}P_{r} = \frac{1}{(r)}$ • Combination: $C(n,r) = {}_{n}C_{r} = {n \choose r} = \frac{1}{r!(r)}$ • Binomial expansion $(a+b)^{n} = \sum_{k=0}^{n} {n \choose k}$ • Pascal's Triangle gives the terms of binomial expansion	 State the definitions of Factorial Permutation Combination Explain why factorials grow very large very quickly. Example: 100! > 9. 3326 × 10¹⁵⁷ Interplain how to simplify Permutations and Combinations to make <i>n</i>! calculating them easier. <i>n</i>-<i>r</i>)! 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Sept.	4	AERO. 5.OA.3 AERO. HSF.BF.2 AERO.HSF. LE.2 AERO.HSF. 1F.3	Patterns, Functions, and Algebra	Chapter 1: Sequences Unit 3: Introduction to Sequences • Definitions o Finite Sequence o Infinite Sequence • Sequence given by o General term o Recursive method (Fibonacci Sequence) • Increasing, decreasing, and bounded sequences	 Define finite and infinite sequences Determine a sequence given a general term. Find the general term given a sample sequence of numbers. Discuss recursive methods Understand and calculate the Fibonacci Sequence Define and identify increasing, decreasing, and bounded sequences. 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Sept Oct.	3		Patterns, Functions, and Algebra	Chapter 1: Sequences Comprehensive Project • Comprehensive group project intended to demonstrate the students comprehensive understanding and functional knowledge of the material from Chapter 1.	 Students will demonstrate their functional knowledge of the material from Chapter 1. 	 Comprehensive Group Project Preferred for the students to do the project outside of class and present their results to the class. 	 Presentation of the Group Project to the class.
Oct.	2		Patterns, Functions, and Algebra	Review for Midterm Exam	 Chapter 1: Sequences Unit 1: Introduction Unit 2: Combinatorics Unit 3: Introduction to Sequences 		
					MIDTERM EXAM		

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Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
Nov.	2	LC.1.C.1	Patterns, Functions, and Algebra	 Chapter 2: Limits Unit 1: Limit of a Sequence Definition Convergent Sequences Special limits Theorem on finite limits Divergent Sequences 	 Define the limit of a sequence Calculate limits of sequences 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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	4	LC.1.C.2 LC.1.C.3 LC.1.C.4 LC.1.C.5	Patterns, Functions, and Algebra	 Chapter 2: Limits Unit 2: Limits of Functions Definition One sided limits Limit Rules The limit exists iff the limit from the right and the limit from the left both exist and are equal. Infinite Limits Rules for limits 	 Define the limit of a function Take simple limits State and use the theorems on limits Define one-sided limits Take one-sided limits Define infinite limits Understand and state the properties on infinite limits Understand and state the rules for infinite limits 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
	2	LC.1.C.6	Patterns, Functions, and Algebra	Chapter 2: Limits Unit 3: Continuous Functions • Definitions • Continuous at a point • Continuous on open or close interval • Discontinuous at a point • Discontinuous on an interval (Supplement) • Basic theorems	 Define what it means for a function to be continuous at a point Define what it means to be continuous on open, closed, and half-open intervals Define what it means to be discontinuous at a point Define what it means to be continuous over an open, closed, or half-open interval State the basic theorems on continuity 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

Grade: 11 (TOEFL-Beginner)

Subject: Mathematics

Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments					
Dec.	3		Patterns, Functions, and Algebra	Chapter 2: Limits Comprehensive Project Comprehensive group project intended to demonstrate the students comprehensive understanding and functional knowledge of the material from Chapter 2.	 Students will demonstrate their functional knowledge of the material from Chapter 2. 	 Comprehensive Group Project Preferred for the students to do the project outside of class and present their results to the class. 	• Presentation of the Group Project to the class.					
	2		Patterns, Functions, and Algebra	Review for Final Exam	 Chapter 2: Limits Unit 1: Limit of a Sequence Unit 2: Limit of a Function Unit 3: Continuous Functions 							

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Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
Jan.	2	D.2.C.1 D.2.C.2 D.2.C.3 D.2.C.4 D.2.C.5	Patterns, Functions, and Algebra	 Chapter 3: Derivatives Unit 1: Introduction to derivatives The slope of the line tangent to a curve Derive the definition of derivative as the slope of a line tangent to a curve Either Lagrange or Leibniz notation is fine, but we normally prefer Leibniz notation: d/dx f(x) = f'(x) 	 Understand the historical problems that led to the development of the derivative Understand and be able to repeat Leibniz's construction of the derivative Understand why we prefer Leibniz's notation over Newton's notation Calculate some basic derivatives using Leibniz's definition of the derivative 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
	5	D.2.C.7	Patterns, Functions, and Algebra	Chapter 3: Derivatives Unit 2: Rules for Taking Derivatives • Derivative Rules • Constant Rule • Power Rule • Sum/Difference Rule • Product Rule • Quotient Rule • Chain Rule • Derivatives of Common Functions • $\frac{d}{dx}x^{-n} = -nx^{-0}$ • $\frac{d}{dx}\sqrt{x} = \frac{\sqrt{x}}{2x}$ • $\frac{d}{dx}\sqrt{f(x)} = (\frac{\sqrt{f(x)}}{2f(x)})\frac{d}{dx}f(x)$	 Take derivatives using the formulas for common functions Take derivatives involving sum, difference, product, and quotient Take derivatives of composite functions 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
Jan Feb.	5	D.2.C.1 D.2.C.2 D.2.C.3 D.2.C.4 D.2.C.5	Patterns, Functions, and Algebra	Chapter 3: DerivativesUnit 3: Derivatives of TrigFunctionsDerivatives of \circ Sin (x) \circ Cos (x) \circ (x)	 Quickly state the derivatives of the basic trig functions Use the derivatives of the basic trig functions to solve word problems. Be able to prove all of the derivative formulas except for sin (x). 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets
Feb.	2		Patterns, Functions, and Algebra	Chapter 3: Derivatives Comprehensive Project Comprehensive group project intended to demonstrate the students comprehensive understanding and functional knowledge of the material from Chapter 3.	 Students will demonstrate their functional knowledge of the material from Chapter 3. 	 Comprehensive Group Project Preferred for the students to do the project outside of class and present their results to the class. 	• Presentation of the Group Project to the class.

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Mar.	2		Patterns, Functions, and Algebra	Review for Midterm Exam	 Chapter 3: Derivatives Unit 1: Introduction to Derivatives Unit 2: Rules for Calculating Derivatives Unit 3: Derivatives of Trig Functions 		
					MIDTERM EXAM		
Mar.	2	AERO HSN.CN.1 AERO HSN.CN.2	Patterns, Functions, and Algebra	Chapter 4: Complex Numbers, Euler's number, and Logarithms Unit 1: Complex Numbers • Definitions • $i = \sqrt{-1}$ • $\mathbb{C} = \{a + bi a, l, l,$	 Understand how complex numbers can be used to solve other types of problems. Understand the applications of complex numbers to modern physics. 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Month	# of Days	Core Standard	Strand	Content	Skills	Activities	Assessments
Mar Apr.	2	AERO. HSF.BF.5. (+)	Patterns, Functions, and Algebra	Chapter 4: e and Logarithms Unit 2: Natural Logarithms • Definition of $e^x = \lim_{n \to \infty} \left(1 + \frac{x}{n}\right)^n$ • Estimate e using the definition above. • Define general logarithms • Define common logarithms • Define Natural logarithms • Rules for natural logarithms	 Recognize common and natural logarithms. Understand the basic concepts of log and exponential functions. Understand how log and exponential functions relate to the real world. 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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Apr.	4	AERO.HSF. 1F.7 AERO.HSA. REI.11	Patterns, Functions, and Algebra	Chapter 4: e and Logarithms Unit 3: Functions with <i>e</i> and <i>ln</i> • Derivatives of • $\frac{d}{dx}e^x = e^x$ • $\frac{d}{dx}\ln x = \frac{1}{x}$ • $\frac{d}{dx}e^{f(x)} = f'(x)e^{-\frac{d}{dx}} \ln f(x) = \frac{f'(x)}{f(x)}$ • Derivatives of other functions involving <i>e</i> and <i>ln</i> . • Euler's • Formula: $e^{ix} = \cos(x) -$ • Identity: $e^{i\pi} = -1$	 Take derivatives for log and exponential functions. Understand and state Euler's formula and Euler's identity Explain the importance of Euler's formula and identity in our modern world. 	 Group Work Mini-Research Projects Computer Projects Worksheets 	 Group Presentations Individual Presentations Worksheets

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	2		Patterns, Functions, and Algebra	Chapter 4: e and Logarithms Comprehensive Project Comprehensive group project intended to demonstrate the students comprehensive understanding and functional knowledge of the material from Chapter 4.	 Students will demonstrate their functional knowledge of the material from Chapter 4. 	 Comprehensive Group Project Preferred for the students to do the project outside of class and present their results to the class. 	• Presentation of the Group Project to the class.
	2		Patterns, Functions, and Algebra	Review for Final Exam	Chapter 4: e and Logarithms Unit 1: Complex Numbers Unit 2: Natural Logarithms Unit 3: Functions with e and In		
FINAL EXAM							